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# Enhancing the Transferability of Adversarial Attacks through Variance Tuning

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# Adversarial Example

Adversarial examples are **indistinguishable** from legitimate ones by adding small perturbations, but lead to **incorrect model prediction**.

**Transferability:** adversarial examples generated for one model can still fool other models, that enables **black-box attacks** in the real-world applications without any knowledge of target model.

**Background:** existing attacks (*e.g.* PGD, CW, etc.) have exhibited great effectiveness, but with **low transferability**.



Raw Image



MI-FGSM



VMI-FGSM



NI-FGSM



VNI-FGSM

Gradient-based adversarial attacks are widely used investigated:

- FGSM [Goodfellow et al., 2015]:

$$x^{adv} = x + \epsilon \cdot \text{sign}(\nabla_x J(x, y; \theta))$$

- I-FGSM [Kurakin et al., 2016]:

$$x_{t+1}^{adv} = x_t^{adv} + \alpha \cdot \text{sign}(\nabla_{x_t^{adv}} J(x_t^{adv}, y; \theta))$$

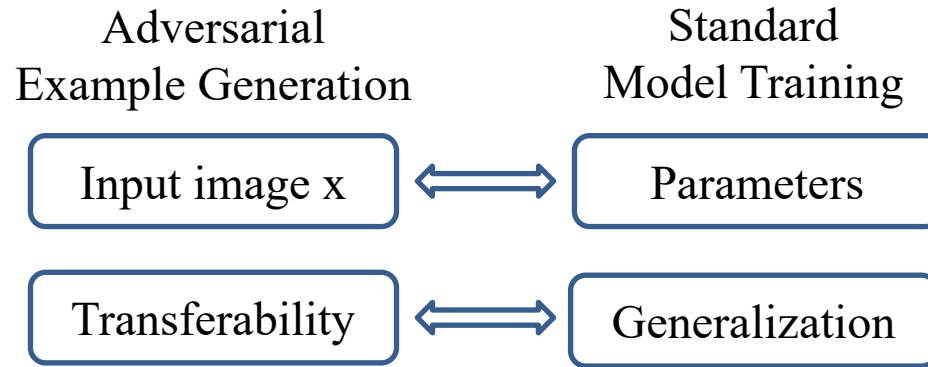
- MI-FGSM [Dong et al., 2018]:

$$g_{t+1} = \mu \cdot g_t + \frac{\nabla_{x_t^{adv}} J(x_t^{adv}, y; \theta)}{\|\nabla_{x_t^{adv}} J(x_t^{adv}, y; \theta)\|_1}, x_{t+1}^{adv} = x_t^{adv} + \alpha \cdot \text{sign}(g_{t+1})$$

- NI-FGSM [Lin et al., 2020]:  $\bar{x}_t^{adv} = x_t^{adv} + \alpha \cdot \mu \cdot g_t$

$$g_{t+1} = \mu \cdot g_t + \frac{\nabla_{\bar{x}_t^{adv}} J(\bar{x}_t^{adv}, y; \theta)}{\|\nabla_{\bar{x}_t^{adv}} J(\bar{x}_t^{adv}, y; \theta)\|_1}, x_{t+1}^{adv} = x_t^{adv} + \alpha \cdot \text{sign}(g_{t+1})$$

Multi-model attack and input transformation based attack are also shown to be effective to improve the transferability.



NI-FGSM finds that Nestorve Accelerated Gradient (NAG) that **accelerates the convergence** of optimization process, also **enhances the transferability**.

We treat the iterative gradient-based adversarial attack as **SGD optimization process**, in which at each iteration, the attacker always chooses the target model for update.

**SGD introduces variance due to randomness.**

**Gradient Variance.** Given a classifier  $f$  with parameters  $\theta$  and loss function  $J(x, y; \theta)$ , an arbitrary image  $x$  and an upper bound  $\epsilon'$  for the neighborhood, the gradient variance can be defined as:

$$V_{\epsilon'}^g(x) = \mathbb{E}_{|x'-x|_p < \epsilon'} [\nabla_{x'} J(x', y; \theta)] - \nabla_x J(x, y; \theta)$$

In practice, we approximate the gradient variance by **sampling  $N$  examples in the neighborhood of  $x$ :**

$$V(x) = \frac{1}{N} \sum_{i=1}^N \nabla_{x^i} J(x^i, y; \theta) - \nabla_x J(x, y; \theta)$$

where  $x^i = x + U[-(\beta \cdot \epsilon)^d, (\beta \cdot \epsilon)^d]$ .

At  $t$ -th iteration, we **tune the gradient of  $x_t^{\text{adv}}$  with the gradient variance at  $(t-1)$ -th iteration** to stabilize the update direction.

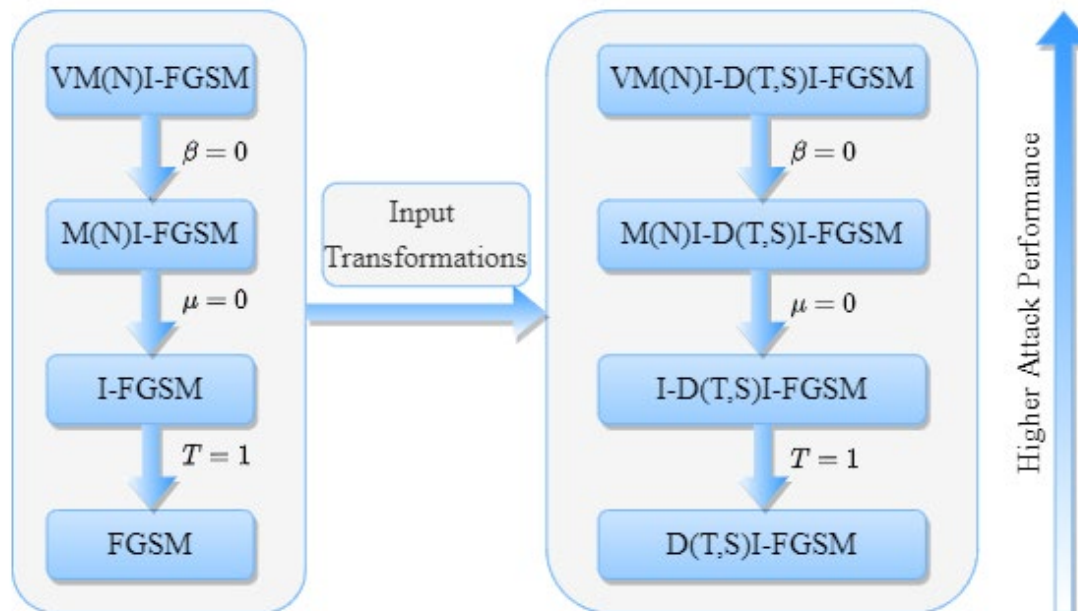
# Variance Tuning

The variance tuning is generally applicable to all iterative gradient based attacks.

VMI-FGSM:

$$g_{t+1} = \mu \cdot g_t + \frac{\nabla_{x_t^{adv}} J(x_t^{adv}, y; \theta) + V(x_{t-1}^{adv})}{\|\nabla_{x_t^{adv}} J(x_t^{adv}, y; \theta) + V(x_{t-1}^{adv})\|_1},$$

$$x_{t+1}^{adv} = x_t^{adv} + \alpha \cdot \text{sign}(g_{t+1})$$



- Dataset: 1,000 clean images from ILSVRC 2012 validation set
- Models: Inc-v3, Inc-v4, IncRes-v2, Res-v2-152
- Defense models:
  - Ensemble AT: Inc-v3<sub>ens3</sub>, Inc-v3<sub>ens4</sub>, IncRes-v2<sub>ens</sub>
  - NIPS 2017 top3 defense: HGD, R&P, NIPS-r3
  - Input transformation: JPEG, Bit-Red, FD, ComDefend
  - Certified defense: RS
  - Denoiser: NRP
- Baselines: MI-FGSM, NI-FGSM, DIM, TIM, SIM
- Attack setting:  $\epsilon = 16$

# Experimental Results

Model	Attack	Inc-v3	Inc-v4	IncRes-v2	Res-101	Inc-v3 <sub>ens3</sub>	Inc-v3 <sub>ens4</sub>	IncRes-v2 <sub>ens</sub>
Inc-v3	MI-FGSM	<b>100.0*</b>	43.6	42.4	35.7	13.1	12.8	6.2
	VMI-FGSM	<b>100.0*</b>	<b>71.7</b>	<b>68.1</b>	<b>60.2</b>	<b>32.8</b>	<b>31.2</b>	<b>17.5</b>
	NI-FGSM	<b>100.0*</b>	51.7	50.3	41.3	13.5	13.2	6.0
	VNI-FGSM	<b>100.0*</b>	<b>76.5</b>	<b>74.9</b>	<b>66.0</b>	<b>35.0</b>	<b>32.8</b>	<b>18.8</b>
Inc-v4	MI-FGSM	56.3	99.7*	46.6	41.0	16.3	14.8	7.5
	VMI-FGSM	<b>77.9</b>	<b>99.8*</b>	<b>71.2</b>	<b>62.2</b>	<b>38.2</b>	<b>38.7</b>	<b>23.2</b>
	NI-FGSM	63.1	<b>100.0*</b>	51.8	45.8	15.4	13.6	6.7
	VNI-FGSM	<b>83.4</b>	99.9*	<b>76.1</b>	<b>66.9</b>	<b>40.0</b>	<b>37.7</b>	<b>24.5</b>
IncRes-v2	MI-FGSM	60.7	51.1	<b>97.9*</b>	46.8	21.2	16.0	11.9
	VMI-FGSM	<b>77.9</b>	<b>72.1</b>	<b>97.9*</b>	<b>67.7</b>	<b>46.4</b>	<b>40.8</b>	<b>34.4</b>
	NI-FGSM	62.8	54.7	<b>99.1*</b>	46.0	20.0	15.1	9.6
	VNI-FGSM	<b>80.8</b>	<b>76.9</b>	<b>98.5*</b>	<b>69.8</b>	<b>47.9</b>	<b>40.3</b>	<b>34.2</b>
Res-101	MI-FGSM	58.1	51.6	50.5	<b>99.3*</b>	23.9	21.5	12.7
	VMI-FGSM	<b>75.1</b>	<b>68.9</b>	<b>70.5</b>	99.2*	<b>45.2</b>	<b>41.4</b>	<b>30.1</b>
	NI-FGSM	65.6	58.3	57.0	99.4*	24.5	21.4	11.7
	VNI-FGSM	<b>79.8</b>	<b>74.6</b>	<b>73.2</b>	<b>99.7*</b>	<b>46.1</b>	<b>42.5</b>	<b>32.1</b>

Table 1: The success rates (%) on seven models in the single model setting by various gradient-based iterative attacks. The adversarial examples are crafted on Inc-v3, Inc-v4, IncRes-v2, and Res-101 respectively. \* indicates the white-box model.



# Experimental Results

Model	Attack	Inc-v3	Inc-v4	IncRes-v2	Res-101	Inc-v3 <sub>ens3</sub>	Inc-v3 <sub>ens4</sub>	IncRes-v2 <sub>ens</sub>
Inc-v3	MI-CT-FGSM	98.7*	85.4	80.6	76.0	64.1	62.1	45.2
	VMI-CT-FGSM	<b>99.3*</b>	<b>88.6</b>	<b>86.7</b>	<b>82.9</b>	<b>78.6</b>	<b>76.2</b>	<b>64.7</b>
	NI-CT-FGSM	98.9*	84.1	80.0	74.5	60.0	56.2	41.0
	VNI-CT-FGSM	<b>99.5*</b>	<b>91.2</b>	<b>89.0</b>	<b>85.3</b>	<b>78.6</b>	<b>76.7</b>	<b>65.3</b>
Inc-v4	MI-CT-FGSM	87.2	98.6*	83.3	78.3	72.2	67.2	57.3
	VMI-CT-FGSM	<b>90.0</b>	<b>98.8*</b>	<b>86.6</b>	<b>81.9</b>	<b>78.3</b>	<b>76.6</b>	<b>68.3</b>
	NI-CT-FGSM	87.8	<b>99.4*</b>	82.5	75.9	65.8	62.6	51.3
	VNI-CT-FGSM	<b>92.1</b>	99.2*	<b>89.2</b>	<b>85.1</b>	<b>80.1</b>	<b>78.3</b>	<b>70.4</b>
IncRes-v2	MI-CT-FGSM	87.9	85.7	<b>97.1*</b>	83.0	77.6	74.6	72.0
	VMI-CT-FGSM	<b>88.9</b>	<b>87.0</b>	97.0*	<b>85.0</b>	<b>83.4</b>	<b>80.5</b>	<b>79.4</b>
	NI-CT-FGSM	90.2	87.0	<b>99.4*</b>	83.2	75.0	68.9	65.1
	VNI-CT-FGSM	<b>92.9</b>	<b>90.6</b>	99.0*	<b>88.2</b>	<b>85.2</b>	<b>82.5</b>	<b>81.8</b>
Res-101	MI-CT-FGSM	86.5	81.8	83.2	<b>98.9*</b>	77.0	72.3	61.9
	VMI-CT-FGSM	<b>86.9</b>	<b>84.2</b>	<b>86.4</b>	98.6*	<b>81.0</b>	<b>78.6</b>	<b>71.6</b>
	NI-CT-FGSM	86.1	82.2	83.3	98.5*	70.0	68.5	54.6
	VNI-CT-FGSM	<b>90.7</b>	<b>85.5</b>	<b>87.2</b>	<b>99.1*</b>	<b>82.6</b>	<b>79.7</b>	<b>73.3</b>

Table 2: The success rates (%) on seven models in the single model setting by various gradient-based iterative attacks enhanced by CTM. \* indicates the white-box model.

# Experimental Results

Attack	Inc-v3	Inc-v4	IncRes-v2	Res-101	Inc-v3 <sub>ens3</sub>	Inc-v3 <sub>ens4</sub>	IncRes-v2 <sub>ens</sub>
MI-FGSM	<b>99.9*</b>	98.2*	95.3*	<b>99.9*</b>	39.4	35.3	24.2
VMI-FGSM	99.7*	<b>98.5*</b>	<b>96.0*</b>	<b>99.9*</b>	<b>67.6</b>	<b>62.9</b>	<b>50.7</b>
NI-FGSM	99.8*	<b>99.8*</b>	<b>98.9*</b>	99.8*	41.0	33.5	23.1
VNI-FGSM	<b>99.9*</b>	99.6*	98.6*	<b>99.9*</b>	<b>71.3</b>	<b>66.0</b>	<b>52.9</b>
MI-CT-FGSM	99.6*	99.1*	97.4*	99.7*	91.3	89.6	86.8
VMI-CT-FGSM	<b>99.7*</b>	<b>99.2*</b>	<b>98.4*</b>	<b>99.9*</b>	<b>93.6</b>	<b>92.4</b>	<b>91.0</b>
NI-CT-FGSM	<b>100.0*</b>	<b>100.0*</b>	<b>100.0*</b>	<b>100.0*</b>	92.8	89.6	83.6
VNI-CT-FGSM	<b>100.0*</b>	99.9*	99.6*	<b>100.0*</b>	<b>95.5</b>	<b>94.5</b>	<b>92.3</b>

Table 3: The success rates (%) on seven models in the multi-model setting by various gradient-based iterative attacks. The adversarial examples are generated on the ensemble models, *i.e.* Inc-v3, Inc-v4, IncRes-v2 and Res-101.

Model	Attack	HGD	R&P	NIPS-r3	Bit-Red	JPEG	FD	ComDefend	RS	NRP	Average
Inc-v3	MI-CT-FGSM	56.6	44.9	52.5	36.2	77.3	60.0	80.1	40.3	29.3	53.0
	VMI-CT-FGSM	<b>73.1</b>	<b>65.1</b>	<b>70.3</b>	<b>49.5</b>	<b>85.4</b>	<b>72.4</b>	<b>86.0</b>	<b>51.9</b>	<b>45.2</b>	<b>66.5</b>
	NI-CT-FGSM	50.4	39.4	47.4	34.3	76.0	58.6	77.7	36.9	24.8	49.5
	VNI-CT-FGSM	<b>73.4</b>	<b>64.5</b>	<b>70.6</b>	<b>51.2</b>	<b>86.8</b>	<b>73.5</b>	<b>87.3</b>	<b>52.1</b>	<b>43.9</b>	<b>67.0</b>
Ens	MI-CT-FGSM	91.0	87.7	89.0	75.9	94.2	88.8	95.1	68.1	76.1	85.1
	VMI-CT-FGSM	<b>92.9</b>	<b>91.0</b>	<b>92.3</b>	<b>80.9</b>	<b>95.4</b>	<b>91.0</b>	<b>96.2</b>	<b>77.0</b>	<b>83.2</b>	<b>88.9</b>
	NI-CT-FGSM	91.3	85.6	89.0	72.3	95.9	89.5	95.4	63.2	69.5	83.5
	VNI-CT-FGSM	<b>94.7</b>	<b>92.4</b>	<b>93.4</b>	<b>82.3</b>	<b>97.1</b>	<b>92.6</b>	<b>97.4</b>	<b>77.4</b>	<b>84.0</b>	<b>90.1</b>

Table 4: The success rates (%) on nine models with advanced defense mechanism by various gradient-based iterative attacks enhanced by CTM. The adversarial examples are generated on Inc-v3 model and the ensemble of models respectively.

- Propose the definition of **gradient variance**.
- Introduce a broad class of iterative gradient based attacks with **variance tuning**.
- Achieve **SOTA** attack transferability on ImageNet against various models with **defenses** in different scenario.



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# Thanks!

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